

### THE LOGIC OF TYPED FEATURE STRUCTURES



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# THE LOGIC OF TYPED FEATURE STRUCTURES

With Applications to Unification Grammars, Logic Programs and Constraint Resolution

**Bob Carpenter** 

Computational Linguistics Program
Philosophy Department
Carnegie Mellon University





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An early source of inspiration was the Unification Categorial Grammar project at the University of Edinburgh, involving Ewan Klein, Mike Reape, Jo Calder, and Henk Zeevat. It was in the context of this project, and in Ewan Klein's introduction to GPSG, that I was first exposed to feature structures. An unpublished paper by Mike Reape was partially responsible for the treatment of extensionality, and Jo Calder's development of typed feature structures was always in the back of my mind.

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viii Acknowledgements

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I originally began thinking about inheritance while working with Rich Thomason at the University of Pittsburgh. It was with his encouragement that I tried to work out connections between knowledge representation formalisms and unification-based linguistic grammar formalisms. Unfortunately, many of the comparisons and contrasts between the inheritance-based feature structure logics presented here and terminological knowledge representation systems such as KL-ONE still remain unclear. Hopefully, this avenue of exploration can be taken up in the future by myself and others. Another task waiting in the wings is the integration of non-monotonic inheritance into the feature structure framework. Recently, foundational work on non-monotonic inheritance has progressed enormously, in part due to the work of the NSF funded LINKUP project involving Dave Touretzky at Carnegie Mellon University, Rich Thomason at the University of Pittsburgh, and Jeff Horty at the University of Maryland.

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