

Lecture Notes in Mathematics

1725

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Dieter A. Wolf-Gladrow

Lattice-Gas Cellular Automata and Lattice Boltzmann Models

An Introduction



Springer

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Cataloging-in-Publication Data applied for

Die Deutsche Bibliothek - CIP-Einheitsaufnahme

Wolf-Gladrow, Dieter:
Lattice gas cellular automata and lattice Boltzmann models : an
introduction / Dieter A. Wolf-Gladrow. - Berlin ; Heidelberg ; New
York ; Barcelona ; Hong Kong ; London ; Milan ; Paris ; Singapore ;
Tokyo : Springer, 2000
(Lecture notes in mathematics ; 1725)
ISBN 3-540-66973-6

Mathematics Subject Classification (1991): 35Q30, 58F08, 65C20, 76P05, 82C40

ISSN 0075-8434
ISBN 3-540-66973-6 Springer-Verlag Berlin Heidelberg New York

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Printed in Germany

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Typesetting: Camera-ready $\text{T}_\text{E}\text{X}$ output by the author
Printed on acid-free paper SPIN: 10700369 41/3143du-543210

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